

St. Anne's Sixth Form Get Ahead Tasks

Maths A Level

Please complete the following questions.

You should aim to complete approximately 75% of the questions form each section.

You should spend 4 or more hours attempting these questions to ensure you are ready for A Level Maths.

Subject Leader: Mrs H Grewal

Exam Board: Edexcel

PREPARATION FOR A LEVEL MATHS BETWEEN YEAR 11 AND YEAR 12.



1)

State the value of each of the following.

(i)
$$2^{-3}$$

(ii)
$$9^0$$
 [1]

2)

(i) Simplify
$$(5a^2b)^3 \times 2b^4$$
. [2]

(ii) Evaluate
$$\left(\frac{1}{16}\right)^{-1}$$
. [1]

3)

Simplify
$$\frac{(3xy^4)^3}{6x^5y^2}$$
. [3]

4)

(i) Write down the value of
$$\left(\frac{1}{4}\right)^0$$
. [1]

(ii) Find the value of
$$16^{-\frac{3}{2}}$$
. [3]

5)

Find the value of
$$\left(\frac{1}{2}\right)^{-5}$$
. [2]

6)

Find the value of
$$\left(\frac{1}{25}\right)^{-\frac{1}{2}}$$
. [2]

7)

Find the value of each of the following, giving each answer as an integer or fraction as appropriate.

(i)
$$25^{\frac{3}{2}}$$
 [2]

(ii)
$$\left(\frac{7}{3}\right)^{-2}$$
 [2]

8)

(i) Evaluate
$$(\frac{9}{16})^{-\frac{1}{2}}$$
. [2]

(ii) Simplify
$$\frac{(2ac^2)^3 \times 9a^2c}{36a^4c^{12}}$$
. [3]

9)

(i) Express
$$125\sqrt{5}$$
 in the form 5^k . [2]

(ii) Simplify
$$(4a^3b^5)^2$$
. [2]

Surds

1)

(i) Simplify
$$\frac{\sqrt{48}}{2\sqrt{27}}$$
. [2]

(ii) Expand and simplify
$$(5 - 3\sqrt{2})^2$$
. [3]

2)

(i) Express
$$\sqrt{75} + \sqrt{48}$$
 in the form $a\sqrt{3}$. [2]

(ii) Express
$$\frac{14}{3-\sqrt{2}}$$
 in the form $b+c\sqrt{d}$. [3]

3)

(i) Simplify
$$\sqrt{98} - \sqrt{50}$$
. [2]

(ii) Express
$$\frac{6\sqrt{5}}{2+\sqrt{5}}$$
 in the form $a+b\sqrt{5}$, where a and b are integers. [3]

4)

(i) Express
$$\sqrt{48} + \sqrt{27}$$
 in the form $a\sqrt{3}$. [2]

(ii) Simplify
$$\frac{5\sqrt{2}}{3-\sqrt{2}}$$
. Give your answer in the form $\frac{b+c\sqrt{2}}{d}$. [3]

5)

(i) Express
$$\frac{1}{5+\sqrt{3}}$$
 in the form $\frac{a+b\sqrt{3}}{c}$, where a,b and c are integers. [2]

(ii) Expand and simplify
$$(3 - 2\sqrt{7})^2$$
. [3]

6)

You are given that
$$a = \frac{3}{2}$$
, $b = \frac{9 - \sqrt{17}}{4}$ and $c = \frac{9 + \sqrt{17}}{4}$. Show that $a + b + c = abc$. [4]

Algebraic fractions

1) Factorise $x^2 - 4$ and $x^2 - 5x + 6$.

Hence express $\frac{x^2 - 4}{x^2 - 5x + 6}$ as a fraction in its simplest form. [3]

2)

Factorise and hence simplify
$$\frac{3x^2 - 7x + 4}{x^2 - 1}$$
. [3]

Proof

1) n is a positive integer. Show that $n^2 + n$ is always even. [2]

2) Prove that, when n is an integer, $n^3 - n$ is always even. [3]

- 3)
 (i) Prove that 12 is a factor of $3n^2 + 6n$ for all even positive integers n. [3]
 - (ii) Determine whether 12 is a factor of $3n^2 + 6n$ for all positive integers n. [2]
- 4) Factorise $n^3 + 3n^2 + 2n$. Hence prove that, when n is a positive integer, $n^3 + 3n^2 + 2n$ is always divisible by 6. [3]

Solving linear inequalities

1) Solve the inequality 6(x+3) > 2x+5. [3]

2) Solve the inequality 3x - 1 > 5 - x. [2]

Solve the inequality $\frac{5x-3}{2} < x+5$. [3]

Solve the inequality $\frac{3(2x+1)}{4} > -6$. [4]

5) Solve the inequality 7 - x < 5x - 2. [3]

Solve the inequality 1 - 2x < 4 + 3x. [3]

Solving equations

Solve the equation $\frac{4x+5}{2x} = -3$. [3]

Solve the equation $\frac{3x+1}{2x} = 4$. [3]

3) Solve the equation $y^2 - 7y + 12 = 0$. Hence solve the equation $x^4 - 7x^2 + 12 = 0$. [4]

4) Solve the equation $4x^2 + 20x + 25 = 0$. [2]

5) Solve the equation $2x^2 + 3x = 0$. [2]

Forming and solving equations

1)

The triangle shown in Fig. 10 has height (x + 1) cm and base (2x - 3) cm. Its area is 9 cm^2 .

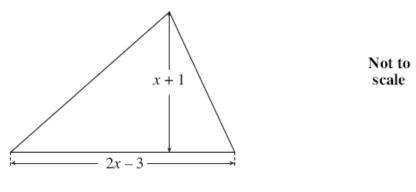


Fig. 10

(i) Show that
$$2x^2 - x - 21 = 0$$
. [2]

(ii) By factorising, solve the equation $2x^2 - x - 21 = 0$. Hence find the height and base of the triangle. [3]

2)

Fig. 9 shows a trapezium ABCD, with the lengths in centimetres of three of its sides.

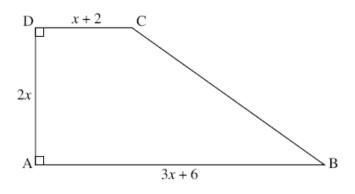


Fig. 9

This trapezium has area 140 cm².

(i) Show that
$$x^2 + 2x - 35 = 0$$
. [2]

(ii) Hence find the length of side AB of the trapezium. [3]

Completing the square and turning points

1)

(i) Express
$$x^2 + 6x + 5$$
 in the form $(x + a)^2 + b$. [3]

(ii) Write down the coordinates of the minimum point on the graph of $y = x^2 + 6x + 5$. [2]

2)

(i) Write
$$x^2 - 7x + 6$$
 in the form $(x - a)^2 + b$.

- (ii) State the coordinates of the minimum point on the graph of $y = x^2 7x + 6$. [2]
- (iii) Find the coordinates of the points where the graph of $y = x^2 7x + 6$ crosses the axes and sketch the graph. [5]

3)

(i) Write
$$3x^2 + 6x + 10$$
 in the form $a(x+b)^2 + c$. [4]

(ii) Hence or otherwise, show that the graph of $y = 3x^2 + 6x + 10$ is always above the x-axis. [2]

4)

(i) Write
$$4x^2 - 24x + 27$$
 in the form $a(x - b)^2 + c$. [4]

- (ii) State the coordinates of the minimum point on the curve $y = 4x^2 24x + 27$. [2]
- (iii) Solve the equation $4x^2 24x + 27 = 0$. [3]
- (iv) Sketch the graph of the curve $y = 4x^2 24x + 27$. [3]

Discriminant and roots

1)

Find the discriminant of $3x^2 + 5x + 2$. Hence state the number of distinct real roots of the equation $3x^2 + 5x + 2 = 0$.

2)

Find the set of values of k for which the equation $2x^2 + 3x - k = 0$ has no real roots. [3]

3)

Find the set of values of k for which the equation $2x^2 + kx + 2 = 0$ has no real roots. [4]

4)

Prove that the line y = 3x - 10 does not intersect the curve $y = x^2 - 5x + 7$. [5]

Changing the subject of a formula

1) Make a the subject of the formula $s = ut + \frac{1}{2}at^2$. [3]

2) The volume of a cone is given by the formula $V = \frac{1}{3}\pi r^2 h$. Make r the subject of this formula. [3]

3) Make y the subject of the formula $a = \frac{\sqrt{y} - 5}{c}$. [3]

4) Rearrange the formula $c = \sqrt{\frac{a+b}{2}}$ to make a the subject. [3]

5) The volume V of a cone with base radius r and slant height l is given by the formula

$$V=\tfrac{1}{3}\pi r^2\sqrt{l^2-r^2}.$$

Rearrange this formula to make *l* the subject.

6) Make a the subject of the equation 2a + 5c = af + 7c.

[4]

[3]

7) Rearrange y + 5 = x(y + 2) to make y the subject of the formula. [4]

8) Make C the subject of the formula $P = \frac{C}{C+4}$. [4]

9) Make x the subject of the formula $y = \frac{1-2x}{x+3}$. [4]

Equation of a straight line

- Find the equation of the line which is parallel to y = 5x 4 and which passes through the point (2, 13).
 Give your answer in the form y = ax + b.
- Find the equation of the line which is parallel to y = 3x + 1 and which passes through the point with coordinates (4, 5).
- Find the equation of the line passing through (-1, -9) and (3, 11). Give your answer in the form y = mx + c.
- A line has equation 3x + 2y = 6. Find the equation of the line parallel to this which passes through the point (2, 10).
- 5)
 (i) Find the equation of the line passing through A (-1, 1) and B (3, 9). [3]
 - (ii) Show that the equation of the perpendicular bisector of AB is 2y + x = 11. [4]

Intersection of two lines

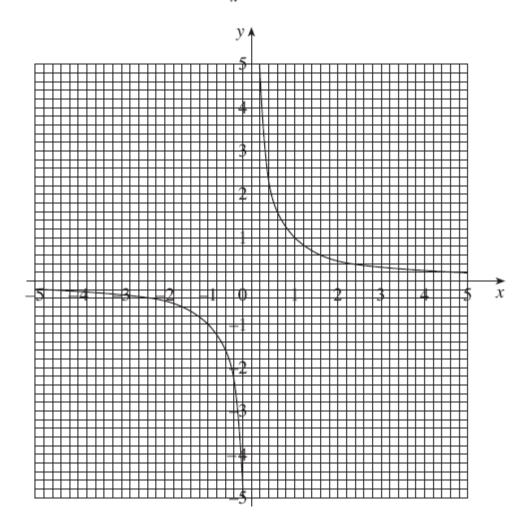
- 1) Find the coordinates of the point of intersection of the lines y = 3x + 1 and x + 3y = 6. [3]
- 2) Find, algebraically, the coordinates of the point of intersection of the lines y = 2x 5 and 6x + 2y = 7. [4]
- Solve the simultaneous equations $y = x^2 6x + 2$ and y = 2x 14. Hence show that the line y = 2x 14 is a tangent to the curve $y = x^2 6x + 2$. [5]
- Find algebraically the coordinates of the points of intersection of the curve $y = 4x^2 + 24x + 31$ and the line x + y = 10. [5]
- Find the coordinates of the points of intersection of the circle $x^2 + y^2 = 25$ and the line y = 3x. Give your answers in surd form. [5]
- A circle has equation $x^2 + y^2 = 45$.
 - (i) State the centre and radius of this circle. [2]
 - (ii) The circle intersects the line with equation x + y = 3 at two points, A and B. Find algebraically the coordinates of A and B.

Show that the distance AB is
$$\sqrt{162}$$
. [8]

Using graphs to solve equations

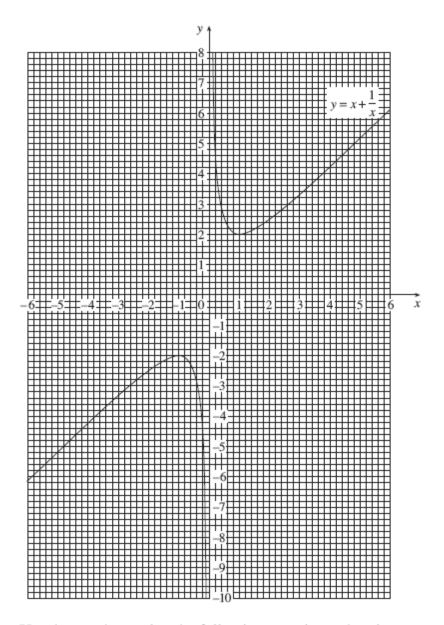
1)

The insert shows the graph of $y = \frac{1}{x}$, $x \neq 0$.



- (i) Use the graph to find approximate roots of the equation $\frac{1}{x} = 2x + 3$, showing your method clearly. [3]
- (ii) Rearrange the equation $\frac{1}{x} = 2x + 3$ to form a quadratic equation. Solve the resulting equation, leaving your answers in the form $\frac{p \pm \sqrt{q}}{r}$. [5]
- (iii) Draw the graph of $y = \frac{1}{x} + 2$, $x \neq 0$, on the grid used for part (i). [2]

The graph of $y = x + \frac{1}{x}$ is shown on the insert. The lowest point on one branch is (1,2). The highest point on the other branch is (-1,-2).



Use the graph to solve the following equations, showing your method clearly.

$$(A) \ x + \frac{1}{x} = 4 \tag{2}$$

(B)
$$2x + \frac{1}{x} = 4$$
 [4]

Transformation of graphs

1)

The point P (5, 4) is on the curve y = f(x). State the coordinates of the image of P when the graph of y = f(x) is transformed to the graph of

(i)
$$y = f(x - 5)$$
, [2]

(ii)
$$y = f(x) + 7$$
. [2]

2)

The curve y = f(x) has a minimum point at (3, 5).

State the coordinates of the corresponding minimum point on the graph of

(i)
$$y = 3f(x)$$
, [2]

(ii)
$$y = f(2x)$$
. [2]

3)

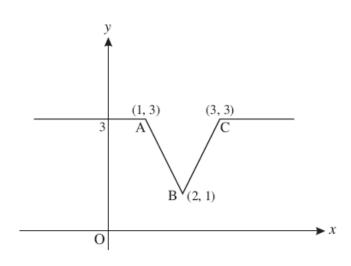


Fig. 4

Fig. 4 shows a sketch of the graph of y = f(x). On separate diagrams, sketch the graphs of the following, showing clearly the coordinates of the points corresponding to A, B and C.

$$(i) y = 2f(x)$$
 [2]

(ii)
$$y = f(x+3)$$
 [2]



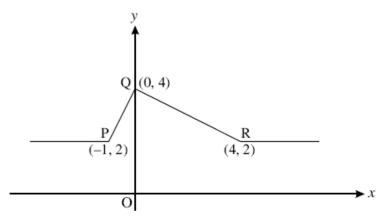


Fig. 5

Fig. 5 shows a sketch of the graph of y = f(x). On separate diagrams, sketch the graphs of the following, showing clearly the coordinates of the points corresponding to P, Q and R.

(i)
$$y = f(2x)$$
 [2]

(ii)
$$y = \frac{1}{4}f(x)$$
 [2]

5)

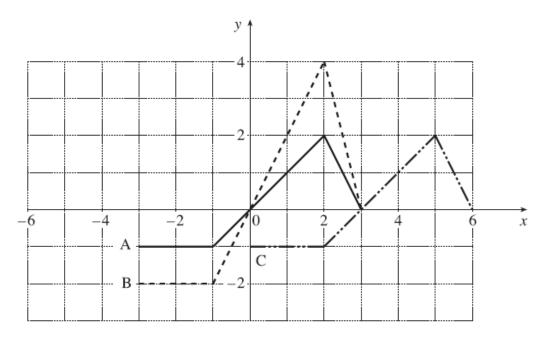


Fig. 3

Fig. 3 shows sketches of three graphs, A, B and C. The equation of graph A is y = f(x).

State the equation of

6) The curve $y = x^2 - 4$ is translated by $\begin{pmatrix} 2 \\ 0 \end{pmatrix}$.

Write down an equation for the translated curve. You need not simplify your answer. [2]

7)

Describe fully the transformation which maps the curve $y = x^2$ onto the curve $y = (x + 4)^2$. [2]

Trigonometric graphs

1) Sketch the curve $y = \sin x$ for $0^{\circ} \le x \le 360^{\circ}$.

Solve the equation $\sin x = -0.68$ for $0^{\circ} \le x \le 360^{\circ}$. [4]

2) Sketch the graph of $y = \cos x$ for $0^{\circ} \le x \le 360^{\circ}$.

On the same axes, sketch the graph of $y = \cos 2x$ for $0^{\circ} \le x \le 360^{\circ}$. Label each graph clearly. [3]

Sine rule and cosine rule

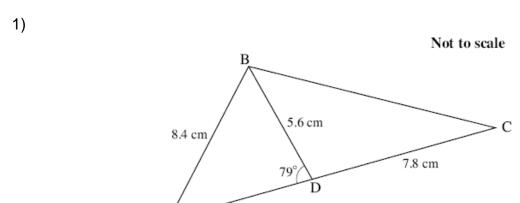


Fig. 7

Fig. 7 shows triangle ABC, with AB = $8.4 \, \text{cm}$. D is a point on AC such that angle ADB = 79° , BD = $5.6 \, \text{cm}$ and CD = $7.8 \, \text{cm}$.

Calculate

(i) angle BAD, [2]

(ii) the length BC. [3]

2)

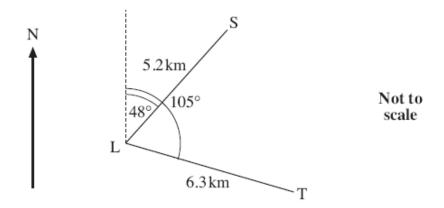


Fig. 10.1

At a certain time, ship S is 5.2 km from lighthouse L on a bearing of 048°. At the same time, ship T is 6.3 km from L on a bearing of 105°, as shown in Fig. 10.1.

For these positions, calculate

Fig. 11.1 shows a village green which is bordered by 3 straight roads AB, BC and CA. The road AC runs due North and the measurements shown are in metres.

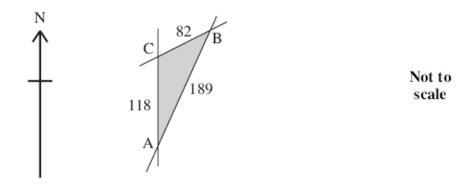


Fig. 11.1

- (i) Calculate the bearing of B from C, giving your answer to the nearest 0.1°. [4]
- (ii) Calculate the area of the village green. [2]

Arc length and sector area

1)
A sector of a circle of radius 18.0 cm has arc length 43.2 cm.

Find the angle of the sector.

[2]

2)

A sector of a circle of radius 5 cm has area 9 cm².

Find the perimeter of the sector.

[5]